

Math 162 - Spring 2025

Workshop 8

Mar 24 - Mar 28

10.1-4 Parametric Equations and Polar Coordinates

Problem 1. $x = \sin(t)$, $y = 1 - \cos(t)$, $0 \leq t \leq 2\pi$

(a) Sketch the curve by using the parametric equations to plot points. Indicate with arrow the direction in which the curve is traced as t increases.

(b) Eliminate the parameter to find a Cartesian equation of the curve.

Problem 2. Find parametric equations for the path of a particle that moves along the circle $x^2 + (y - 1)^2 = 4$ in the manner described.

(a) Once around clockwise, starting at $(2, 1)$

(b) Three times around counterclockwise, starting at $(2, 1)$

(c) Halfway around counterclockwise, starting at $(0, 3)$

Problem 3. $x = t - \ln(t)$, $y = t + \ln(t)$

Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$. For which values of t is curve concave upward?

Problem 4. Identify the curve by finding a Cartesian equation for the curve

(a) $r = 4\sec(\theta)$, (b) $r^2\sin(2\theta) = 1$ (c) $r = 5\cos(\theta)$

Problem 5. Find a polar equation for the curve represented by the given Cartesian equation.

(a) $y = \sqrt{3}x$, (b) $y = -2x^2$, (c) $x^2 + y^2 = 4y$

Problem 6. Find the area of the region that lies inside both curves

(a) $r = 3\sin(\theta)$, $r = 3\cos(\theta)$

(b) $r = 1 + \cos(\theta)$, $r = 1 - \cos(\theta)$

Problem 7. Find the exact length of the polar curve.

(a) $r = e^{\theta/2}$, $0 \leq \theta \leq \pi/2$

(b) $r = 2(1 + \cos(\theta))$