

Warm-up:

1. Trigonometry review:
  - (a) Draw two reference triangles,  $30 - 60 - 90$  and  $45 - 45 - 90$ , and label side lengths and angles in radians.
  - (b) What are  $\cos(\pi/4)$ ,  $\cos(\pi/6)$ ,  $\sin(\pi/6)$ ,  $\tan(\pi/3)$  and  $\tan(\pi/4)$ ?
  - (c) What are  $\cos(5\pi/6)$ ,  $\cos(7\pi/6)$ , and  $\tan(11\pi/6)$ ?
  - (d) Find all angles  $\theta$  with  $\cos(\theta) = 1/2$ .
  - (e) Find all angles  $\theta$  with  $\sin(\theta) = \frac{-1}{\sqrt{3}}$ .
  - (f) Sketch the graph in the  $r, \theta$  plane of  $r = \sin(2\theta)$ .
  - (g) Sketch the graph in the  $r, \theta$  plane of  $r = 5 - 2\sin(\theta)$ .

Problems:

1. Let

$$x = \frac{1 - t^2}{1 + t^2}, \quad y = \frac{2t}{1 + t^2}.$$

- (a) Sketch this as  $t$  increases from  $-2$  to  $2$ .
  - (b) What happens to  $x$  and  $y$  as  $t \rightarrow \infty$ . What about as  $t \rightarrow -\infty$ .
  - (c) show that this parametric curve traces out the circle  $x^2 + y^2 = 1$ .
  - (d) Compute  $dy/dx$  for this curve, first by using  $x^2 + y^2 = 1$ , then using the parametric equations.
  - (e) Find an equation for the tangent line to the curve at  $t = 2$ .
2. Sketch the following parametric curves:
  - (a)  $x = \sin(4\theta)$ ,  $y = \cos(4\theta)$ ,  $0 \leq \theta \leq \pi/2$
  - (b)  $x = 2^t - t$ ,  $y = 2^{-t} + t$ ,  $-3 \leq t \leq 3$
  - (c)  $x = \cos^2(t)$ ,  $y = 1 + \cos(t)$ ,  $0 \leq t \leq \pi$

3. Match the following parametric equations to their graphs

$x = \cos(t), y = \sin(t), 0 \leq t \leq \pi$	$x = \cos(3t), y = \sin(2t), 0 \leq t \leq 2\pi$	$x = t^2, y = t^5, -1 \leq t \leq 1$
$x = \cos(2t), y = \sin(2t), 0 \leq t \leq \pi$	$x = t + \cos(2t), y = t + \sin(2t), 0 \leq t \leq \pi$	$x = t^5, y = t^2, -1 \leq t \leq 1$
$x = 3 \cos(t), y = 2 \sin(t), 0 \leq t \leq 2\pi$	$x = 2 \cos^2(t), y = 3 \sin^2(t), 0 \leq t \leq 2\pi$	$x = t^2 - t, y = t^2 + t, 0 \leq t \leq 2$
$x = 2 \cos(t), y = 3 \sin(t), 0 \leq t \leq 2\pi$	$x = 1 - \sin(t), y = \cos^2(t), 0 \leq t \leq 2\pi$	$x = t^3 + t^2 - t, y = t^2 - t^4, -1 \leq t \leq 1$

Graphs:

